

Magnetic structure and spin dynamics of quasi-one-dimensional spin-chain antiferromagnet $\text{BaCo}_2\text{V}_2\text{O}_8$

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We report a neutron diffraction and muon spin relaxation μ SR study of static and dynamical magnetic properties of $\text{BaCo}_2\text{V}_2\text{O}_8$, a quasi-one-dimensional spin-chain system. A proposed model for the antiferromagnetic structure includes: a propagation vector $\vec{k}_{AF} = (0, 0, 1)$, independent of external magnetic fields for fields below a critical value $H_c(T)$. The ordered moments, of $2.18 \mu_B$ per Co ion, are aligned along the crystallographic c -axis. Within the screw chains, along the c axis, the moments are arranged antiferromagnetically. In the basal planes the spins are arranged ferromagnetically (forming zig-zags paths) along one of the axis and antiferromagnetically along the other. The temperature dependence of the sub-lattice magnetization is consistent with the expectations of the 3D Ising model. A similar behavior is observed for the internal static fields at different muon stopping sites. Muon time spectra measured at weak longitudinal fields and temperatures much higher than T_N can be well described using a single muon site with an exponential muon spin relaxation that gradually changes into an stretched exponential on approaching T_N . The temperature-induced changes of the relaxation suggest that the Co fluctuations dramatically slow down and the system becomes less homogeneous as it approaches the antiferromagnetic state.

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INTRODUCTION

One-dimensional (1D) spin chain systems with nearest-neighbor antiferromagnetic (AF) exchange interactions have attracted much attention in the last decades because they display a rich variety of ground states with non-classical magnetic phenomena.[1–3] It is well known that an ideal 1D AF spin system does not undergo long-range order (LRO) at finite temperatures due to strong quantum spin fluctuations.[4] But slight perturbations of the system by, for instance, weak interchain interactions or doping with non-magnetic impurities, can make the quantum critical state unstable and favors three-dimensional (3D) AF LRO.[5, 6]

In 2005 $\text{BaCo}_2\text{V}_2\text{O}_8$, a new member of the quasi-1D AF spin-chain family, was synthesized by Zhangzhen He and co-workers.[7–9] They succeeded in growing large single crystals of high quality. $\text{BaCo}_2\text{V}_2\text{O}_8$ is an insulator with a very anisotropic magnetic susceptibility χ ; the easy axis of magnetization is along the crystallographic c axis. The temperature dependence of the magnetic susceptibility $\chi(T)$ displays a broad maximum near 30 K signaling the development of 1D short-range order.[7]

Crystal-field effects and spin-orbit coupling partially lift the degeneracy of the single ion $\text{Co}^{2+}(3d^7)$ multiplet

resulting in a doublet ground state. Thus the spin-system may be considered as a collection of effective $S = 1/2$ spin chains.[10] With lowering temperature, a rapid drop of χ at $T_N = 5.4$ K signals the onset of a long-range ordered AF state at zero field.[7] Quantum fluctuations of the spins strongly affect the ordered state, as evidenced by the phenomena observed in external fields applied parallel to the chains, which results in an unusual field-temperature phase diagram (see Fig. 1).

The magnetization curves $M(H)$ are strongly non-linear.[10–12] External magnetic fields H above a critical value $H_c(T)$ suppress the 3D AF Néel state. At $T = 0$ K, $\mu_0 H_c = 3.9$ T. The field-induced suppression of the Néel state occurs in an unusual manner. Above 1.8 K, H induces a reentrant phenomenon from the long-range 3D, Néel state into a 1D quantum liquid state (order-disorder transition).[13] This transition was theoretically predicted first for gapped spin systems doped with non-magnetic impurities.[14]

At lower temperatures, however, external fields $H \geq H_c(T)$ result in the development of an incommensurably modulated AF state. The existence of this novel phase was demonstrated experimentally by Kimura and co-workers.[15–18] They found for the modulated structure a propagation vector $\vec{k}_M = (0, 0, 1 + \delta)$ with δ tunable by

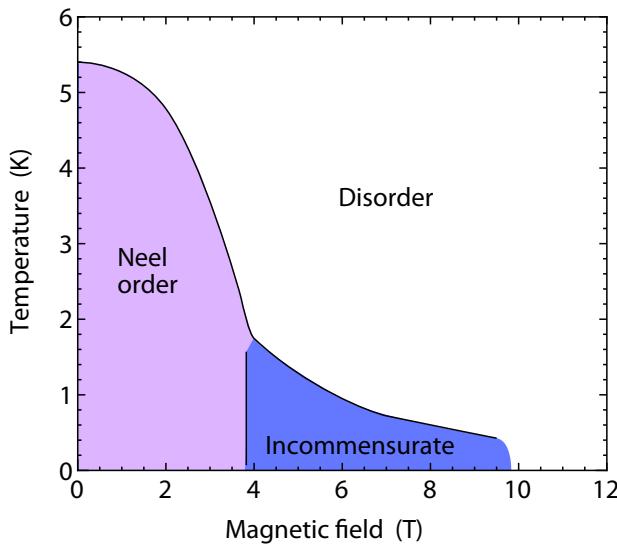


FIG. 1: Schematic representation of the Magnetic Field - Temperature phase diagram of $\text{BaCo}_2\text{V}_2\text{O}_8$ for fields applied along the c -axis. Two magnetically ordered phases are distinguished: (i) The Néel state, a 3D AF state at low fields, and (ii) an incommensurably modulated phase at higher fields (from Kimura and co-workers, Ref. 17).

the external magnetic field.

Although many interesting properties have been investigated in $\text{BaCo}_2\text{V}_2\text{O}_8$, there are no reports on the details of the structure of the Néel ordered state, *i.e.*, in external magnetic fields $H < H_c(T)$. In addition, there is very little information about the spin dynamics in this system, except for two NMR studies.[19, 20] We present here a detailed model for the magnetic structure, obtained from neutron diffraction measurements in powder samples and in single crystals of this material. We also report the results of μSR measurements below and above T_N . The latter shine light into the dynamics of the spin system.

The physical properties of $\text{BaCo}_2\text{V}_2\text{O}_8$ can be understood in the context of Ising spin chains with weak interchain interactions as described by the $S = 1/2$, XXZ model where a single chain in the presence of an external magnetic field H is described by the Hamiltonian

$$\mathcal{H} = J \sum_i (S_i^z S_{i+1}^z + \epsilon (S_i^x S_{i+1}^x + S_i^y S_{i+1}^y)) - g\mu_B \sum_i S_i^z H \quad (1)$$

From magnetization and ESR data it has been determined for $\text{BaCo}_2\text{V}_2\text{O}_8$ that the AF exchange interaction is $J/k_B = 65$ K, the anisotropy parameter $\epsilon \approx 0.5$, and $g \approx 6.2$. The interchain interaction J' is of the order of $J'/J \approx 0.06$.[11] In this model Néel order occurs at zero field with a non-vanishing gap.[5] The application of external magnetic fields, $H > H_c$, restores the Tomonaga-Luttinger spin-liquid state with longitudinal and transversal incommensurate spin fluctuations that

characterize 1D Ising systems.[2, 21]

$\text{BaCo}_2\text{V}_2\text{O}_8$ crystallizes adopting a tetragonal structure with space-group symmetry $I41/acd$, room-temperature lattice parameters of $a = 12.444\text{\AA}$ and $c = 8.415\text{\AA}$ and 8 formula units per unit cell. All the magnetic Co ions are equivalent. They lie in the centers of CoO_6 octahedra, and have strong AF exchange interactions with Co ions in the neighboring edge-sharing CoO_6 octahedra. The Co^{2+} spins, here referred simply as "spins", form a collection of screw-type chain structures along the c axis. The screw chains are separated by nonmagnetic VO_4 (V^{5+}) and BaO_4 (Ba^{2+}) tetrahedra, resulting in a quasi-one-dimensional structural arrangement of the spins with a strong Ising-type magnetic anisotropy. A representation of the crystal structure is given in Fig. 2.

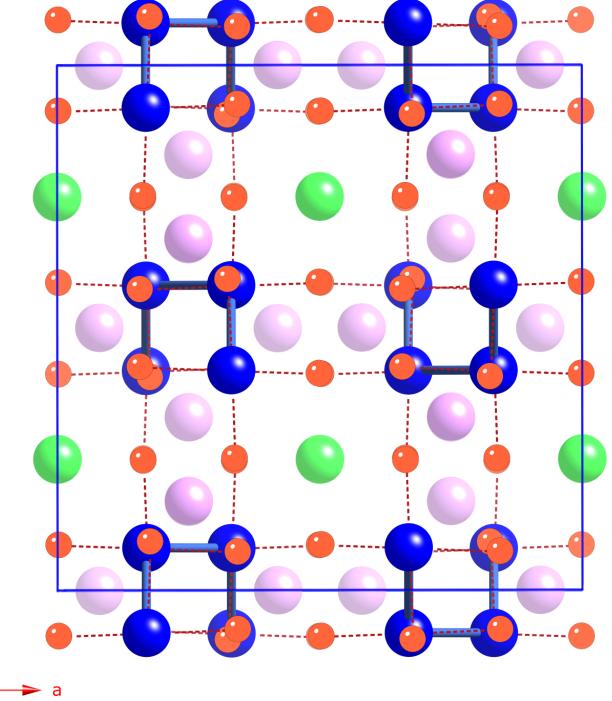


FIG. 2: Representation of the basal plane projection of the crystal structure of $\text{BaCo}_2\text{V}_2\text{O}_8$. This figure emphasizes large blue circles, representing Co ions with the rods joining them representing the n.n. Co-Co bonds. The small orange circles represent the O ions, the green and violet circles represent the Ba and V ions, respectively (colors on line).

EXPERIMENTAL PROCEDURE

Polycrystalline samples of $\text{BaCo}_2\text{V}_2\text{O}_8$ were synthesized by a standard solid-state reaction method using high purity reagents of BaCO_3 (4N), $\text{CoC}_2\text{O}_4 \cdot 2\text{H}_2\text{O}$ (3N)

and V_2O_5 (4N) as starting materials. Single crystals of $\text{BaCo}_2\text{V}_2\text{O}_8$ (of dimensions of the order of $10 \times 8 \times 3$ mm³) were grown by a spontaneous nucleation method from the same starting materials. Details of the material synthesis have been previously described.[7, 8, 12] Our material was characterized by X-ray diffraction and magnetic susceptibility. The crystal structure and the magnetic properties confirmed the conclusions based on previous data.[13]

The magnetic structure of $\text{BaCo}_2\text{V}_2\text{O}_8$ in zero external magnetic field was investigated by measuring neutron powder diffraction patterns at temperatures down to 1.8 K using incident neutrons of wavelength of 2.4503 Å in the Cold Neutron Powder Diffractometer DMC at SINQ, Paul Scherrer Institute (PSI), Switzerland. The sample consisted of 8 g of powdered $\text{BaCo}_2\text{V}_2\text{O}_8$ material enclosed in a thin-walled V cylindrical container. On a single crystalline sample, we measured the temperature and field dependencies of some selected magnetic Bragg reflections using the Triple Axis Spectrometer Rita-II and the Thermal Single Crystal Diffractometer TriCS both at SINQ, PSI. The latter with incident neutrons of a wavelength $\lambda = 1.18\text{\AA}$. External magnetic fields, of up to $\mu_0 H = 4.5$ T, were applied along c axis. μSR time spectra were measured on a polycrystalline sample, in the temperature range between 1.5 and 100 K in zero and weak longitudinal magnetic fields, using the General Purpose Surface-Muon Instrument GPS at the Swiss Muon-Source of PSI.

RESULTS AND DISCUSSION

Magnetic structure

In Figs. 3(a) and 3(b) we display neutron powder diffraction patterns above (8 K) and below (1.3 K) the Néel temperature, respectively. The magnetic Bragg reflections, *i.e.*, the difference of intensities [$I(1.3 \text{ K}) - I(8 \text{ K})$] is displayed in Fig. 3(c). A refinement using the "FullProf" software package [22] yielded a very good fit of all the magnetic and nonmagnetic reflections. From the nuclear reflections we obtained for the lattice parameters of the tetragonal cell at 8 K: $a = 12.389$ Å and $c = 8.375$ Å. All the magnetic reflections, which appear below T_N , could be indexed in the tetragonal system with a wave vector $\vec{k}_{AF} = (0, 0, 1)$. The best fit to the data are represented by solid lines in Figs. 2(a)-2(c), where the conventional Rietveld factors are $R_p = 6.08$, $R_{wp} = 6.13$ and $R_{exp} = 1.13$.

The refined spin structure is represented in Fig. 4, where the Co ions are depicted as circles and their bonds as the heavy solid lines joining them. Different coordinates along the c axis are indicated by the different fillings of the circles. This figure emphasizes the parts of the screw chains contained within the unit cell. The

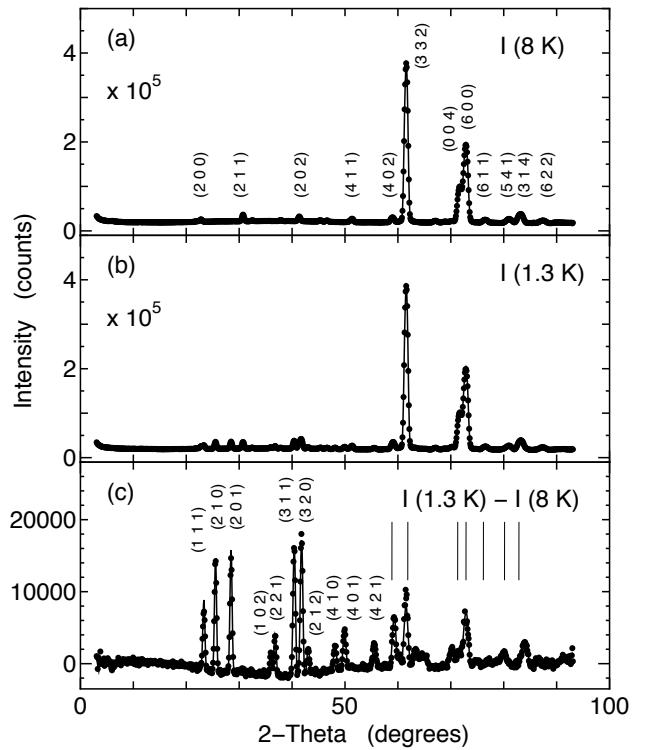


FIG. 3: Bragg scattering profiles for $\text{BaCo}_2\text{V}_2\text{O}_8$ at $T = 8$ K (a) and $T = 1.3$ K (b). A pattern corresponding to the difference of intensities [$I(1.3 \text{ K}) - I(8 \text{ K})$] and revealing only the magnetic Bragg reflections is shown in (c). The solid lines represent the refinement of the data using a model described in the text.

chains run along the c -axis, the ordered Co moments are aligned along the same direction and "u" and "d" represent up and down spin directions. The spins are arranged antiferromagnetically along the screw chains, but at a given basal plane they are arranged antiferromagnetically (ferromagnetically) forming zig-zag paths along the a (b) axis. The Bragg peaks are very narrow, resolution limited, thus, the 3D long-range character of the AF order is confirmed. From the refinement, the magnitude of Co moments is estimated to be $2.18 \mu_B$ which for an effective spin $S = 1/2$ implies an effective g -factor of $g \approx 4.4$.

Our neutron powder-diffraction data are not compatible with the value $g = 6.2$, obtained from high-field ESR and magnetization results.[7] Assuming the ESR g -value, the calculated intensities of the magnetic reflections would be too large, by a factor of 2, to fit the experimental data. Therefore, we conclude that the Néel state involves reduced Co moments. This reduction is probably due to quantum fluctuations expected in the 3D XXZ model. But the discrepancy of the g -factors extracted from neutron scattering, high-field ESR and magnetization results have to be considered carefully since these techniques probe the spin system under different condi-

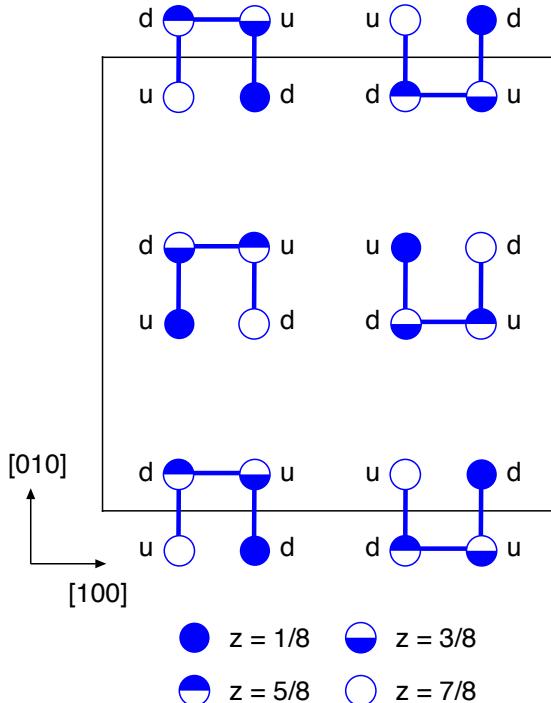


FIG. 4: Representation of the magnetic structure of $\text{BaCo}_2\text{V}_2\text{O}_8$ in the AF state. Co ions are depicted as circles and their bondings as solid lines. The quasi-1D screw-type spin chains run along the c -axis and the "up" and "down" spin directions are represented by "u" and "d", respectively.

tions.

We have measured the temperature and field dependences of selected magnetic Bragg reflections on a single crystalline sample using Rita-II. A summary of these results is presented in Fig. 5. The circles in the main panel represent the square root of the integrated magnetic Bragg intensity $\sqrt{I_B}$ of the $(3, 2, 0)$ reflection as a function of temperature. This quantity is proportional to the sublattice magnetization. Its functional form, *i.e.*, the $\sqrt{I_B}(T)$ curve, follows the expectations for a 3D Ising antiferromagnet, here represented by the solid line. In a limited temperature range near T_N ($0.8 \leq T/T_N \leq 1$), we find

$$\sqrt{I_B} \propto (1 - T/T_N)^\beta. \quad (2)$$

The fits to the data using Eq. (2) yielded a Néel temperature $T_N = 5.4$ K, as expected, and a critical exponent $\beta = 0.28$. This value is close to the predictions of the 3D Ising model, which has been estimated to be $\beta \approx 5/16$, with the exact value depending slightly on the approximations used. For the 2D case: $\beta = 1/8$.[23–26]

The inset of Fig. 5 shows the normalized integrated intensity of three magnetic Bragg reflections $(2, 1, 0)$, $(4, 1, 0)$ and $(3, 2, 0)$ as a function of magnetic field along the c axis. For comparison, we also plot the intensity of the nuclear Bragg reflection $(2, 0, 0)$. The data indicate that

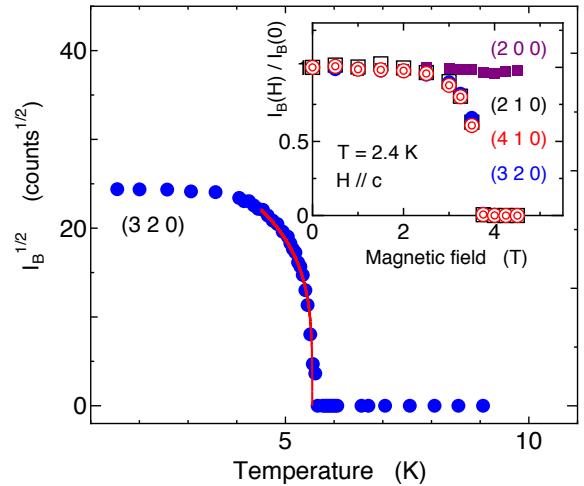


FIG. 5: The temperature dependence of the square root of the integrated intensity of the $(3, 2, 0)$ magnetic reflection. The inset shows the magnetic field dependence of Bragg intensity of $(2, 1, 0)$, $(4, 1, 0)$, $(3, 2, 0)$ magnetic reflections and the nuclear $(2, 0, 0)$ as a function of magnetic field along the c axis.

the magnetic ordering is suppressed by external magnetic fields of 3.75 T along the c axis, at 2.4 K. This is in agreement with the results obtained from measurements of the specific heat in external magnetic fields.[8, 11] We found no measurable field dependence for the magnetic propagation vector k_{AF} in the Néel ordered phase.

In an effort to add more light to the nature of the phase transition into the spin liquid phase, we have searched for quasi-elastic scattering in the vicinity of the above mentioned magnetic Bragg reflections. The searches were performed at temperatures near T_N and zero external magnetic field using the thermal single crystal diffractometer TriCS with a 2D detector, at SINQ, PSI. No clear quasi-elastic signals were detected.

Muon spin relaxation and rotation

To investigate the spin dynamics of $\text{BaCo}_2\text{V}_2\text{O}_8$ in the paramagnetic state, we have performed μ SR experiments in zero-field ZF and in weak longitudinal external magnetic-fields LF.[27] Four typical μ SR spectra above T_N , measured in a field of 20 Oe are shown in Fig. 6. This weak external field effectively suppresses the contribution to the muon relaxation due to quasi-static nuclear dipolar fields. This leaves basically a dynamical relaxation, which for the case of a single relaxation rate is usually well described by a simple exponential function.[28] More complex dynamic cases are described using stretched exponential functions.[29, 30]

The LF- μ SR time spectra data above T_N were fitted

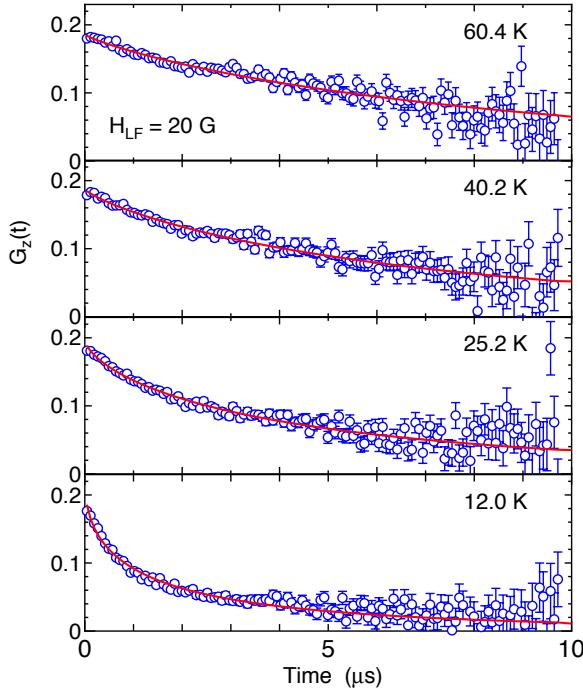


FIG. 6: μ SR time spectra measured in a weak longitudinal external magnetic field, of 20 G, in the paramagnetic state at four temperatures well above T_N . The data points represent the time spectrum $G_z(t)$ versus Time (μ s) for temperatures 60.4 K, 40.2 K, 25.2 K, and 12.0 K. The solid lines represent fits to the data using effectively a single component (see text).

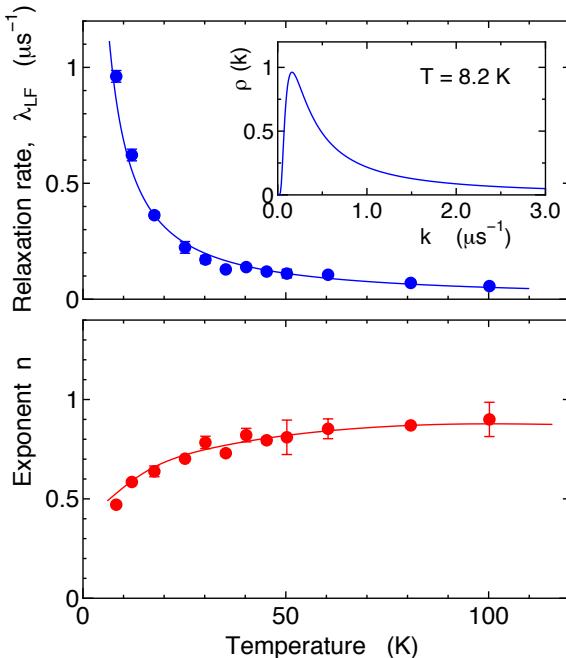


FIG. 7: Temperature dependence of muon relaxation rate λ_{LF} (a) and stretched exponent n (b) obtained in a external longitudinal field of 20 G in the paramagnetic state. The inset in (a) depicts the distribution of relaxation rates at $T \approx 8$ K, where $n = 0.5$ (see text).

using

$$G_z(t) = A \exp[-(\lambda_{LF} t)^n], \quad (3)$$

where A is the initial asymmetry and λ_{LF} is a parameter also denoted here as the muon longitudinal spin relaxation rate. The best fits are represented by the solid lines in Fig. 6. In the paramagnetic state the relaxation (of dynamic character) is associated with the fluctuations of the Co moments. An stretched exponent $n \approx 1$ reveals a sharp distribution of rates, which effectively may be represented by a single spin relaxation rate λ_{LF} for the entire spin system, while smaller values, $n < 1$, suggests a distribution of rates which rapidly broadens with decreasing n . Only two parameters are needed to fully describe the distribution of rates: The (stretched) exponent n characterizes the width of the distribution and $1/\lambda_{LF}$ is the time needed for the initial asymmetry A to decay to $1/e$ of its initial value (independent of n).

The results of the temperature dependence of λ_{LF} and n are summarized in Figs. 7(a) and 7(b). At high temperatures, $T > 30$ K, the data are well fitted with a stretched exponent $n \approx 1$, signaling that the system is rather homogeneous. Below 30 K, with decreasing temperature, $\lambda_{LF}(T)$ displays a substantial increase suggesting a rapid slowing down of the dynamics of the Co spin fluctuations. These are considered as in the "fast fluctuation regime" at all temperatures of these particular measurements, $T > 8$ K. At the same time the system becomes more inhomogeneous, as judged by the rapid decrease of n . At 100 K, $n \approx 0.9$ but just above T_N , $n \approx 0.5$. The increase of λ_{LF} with decreasing T is associated with the increase of AF correlations among Co moments within the individual screw chains. This claim obtains support from previous findings based on results for $\chi(T)$. A broad maximum in $\chi(T)$ signals the onset of intra-chain magnetic correlations.[8] An illustration of the inhomogeneity of the system at low temperatures is given by the distribution of rates depicted in the inset of Fig. 7(a).

Stretched exponential relaxation appears in a wide variety of phenomena,[29] including spin glasses and AF systems with frustrated interactions. In such systems, the relaxation at high temperatures follows an exponential form and, as the temperature decreases (towards the freezing temperature in spin glasses), the functional form changes into a stretched exponential function[30]

$$G_z(t) = A \exp[-(\lambda t)^{\frac{d}{d+2}}]. \quad (4)$$

Here the stretched exponent depends on the effective dimensionality d . Qualitatively this general picture applies to our system with a reduced dimensionality, since already at 8.2 K, Fig. 7(b) shows that $n \leq 0.5$, clearly below the expectations for a 3D case ($n \leq 3/5$). There is a clear trend of decreasing n with decreasing temperature. At low temperatures the tendency seems to be

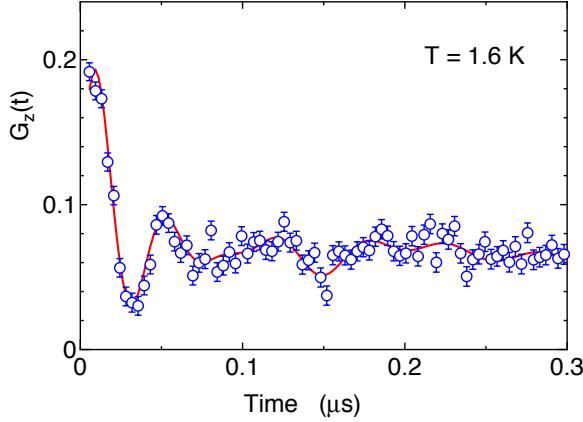


FIG. 8: μ SR time spectrum measured in zero field in the AF state at 1.6 K . The solid line represents a fit to the data using 5 different components.

$n \rightarrow 1/3$, *i.e.*, towards the $d = 1$ case. But this trend changes abruptly upon ordering, where the effective dimensionality of the system suddenly transforms into 3D.

In Fig. 8 we present the ZF- μ SR time spectrum at $T = 1.6 \text{ K}$, deep in the AF state. Here a spontaneous Larmor precession is revealed by the time-evolution of the asymmetry. The prominent structures revealed in this plot signal the presence of several inequivalent muon sites with non-vanishing internal static fields. This is characteristic of a magnetically ordered state.

The muon spectrum below T_N is well described by assuming four components with different relaxation rates and different Larmor frequencies:

$$G_z(t) = A \exp(-\lambda t) + \sum_{i=1}^4 A_i \exp(-\lambda_i t) \cos(2\pi\nu_i t + \phi), \quad (5)$$

where the first term, a signal with vanishing Larmor frequency, is associated with muons whose spins are oriented along the internal static fields. This corresponds to $1/3$ of the total signal for our polycrystalline sample, *i.e.*, $A \approx 1/3(A + A_1 + A_2 + A_3 + A_4)$. Therefore, the contribution to the asymmetry from muon sites with vanishing static magnetic dipolar field must be small, otherwise the fraction of A relative to the total asymmetry would be larger. The signals with non-vanishing Larmor frequencies: $\nu_1 = 5.7$, $\nu_2 = 11.1$, $\nu_3 = 18.4$ and $\nu_4 = 23.9$ MHz, at 1.6 K , arise from muon stopped at sites with internal static fields of 0.42 , 0.82 , 1.36 and 1.76 kOe, respectively. The largest asymmetry is 0.12 corresponding to ν_4 and is substantially larger than the other signals ($A_4 \gg A_1 \sim A_2 \sim A_3$). Muon motion in the crystal may be ruled out by the lack of appreciable temperature-induced changes in the asymmetries A_1, A_2, A_3 and A_4 below T_N .

The model described by Eq. (5) is plausible. For instance, the largest relaxation rate corresponds to the

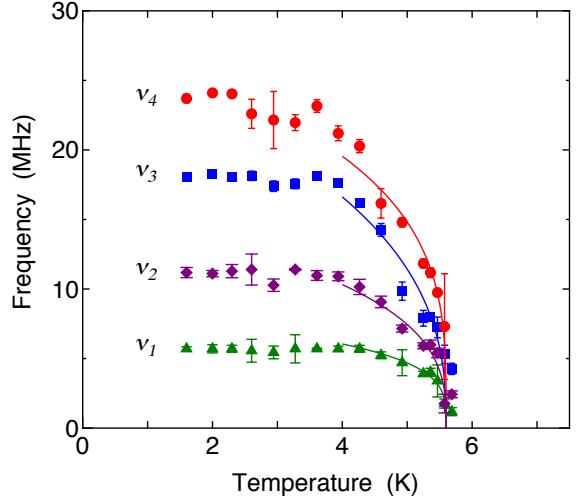


FIG. 9: Temperature dependence of non-zero muon relaxation frequencies inferred from the zero-field data in the AF state. All the frequencies vanish at $T_N = 5.4 \text{ K}$. The solid lines represent fits to the data using the 3D Ising model.

largest internal fields; $\lambda_4 \approx 28$ MHz. The other three have substantially smaller relaxation rates, of the order of $\lambda_1 \sim \lambda_2 \sim \lambda_3 \sim 7$ MHz. The lowest rate corresponds to the signal with vanishing Larmor frequency $\lambda < 0.8$ MHz. Although the model yields good fits of the data it has limitations; namely, it is difficult to identify the muon sites. We found several interstitial sites, (x, y, z) with $x/a, y/b, z/c = \{0, 0.5\}$, where the electric field vanishes. However, at these sites the calculated dipolar magnetic field also vanishes and, therefore, they are unlikely to contribute to the observed asymmetry. Muon sites where the dipolar magnetic field correspond to the inferred internal static fields are, for instance, near the centers of sides and faces of some BaO_4 tetrahedra. However, at these places the electric field does not vanish. We conclude that most likely the observed signals must arise from muon bound to oxygen ions.

In Fig. 9 we display the temperature dependence of the non-zero muon Larmor frequencies inferred from the zero-field data. All the frequencies vanish as T approaches T_N . The solid lines represent fits to the data using the critical behavior $\nu = \nu_0(1 - (T/T_N)^\beta)$. Experimentally one finds $\beta \sim 0.28$, similar to the value obtained in the analysis of the neutron diffraction data, and close to the expectations of the 3D Ising model. Therefore, below T_N the data consistently suggest that the ordered moments of $\text{BaCo}_2\text{V}_2\text{O}_8$ may be considered as a 3D Ising system.

In summary, as $\text{BaCo}_2\text{V}_2\text{O}_8$ approaches the antiferromagnetic state with decreasing temperatures: (i) the Co moment fluctuations undergo a drastic slowing down and (ii) the system, as probed by the muon relaxation, becomes gradually inhomogeneous. These features reflect the development of 1D intra-chain AF correlations

and show that just above T_N the dynamics of the spin system may be thought of as a disordered Ising system with reduced dimensionality (probably 1D). The phase transition at T_N may be thought of as the order-disorder transition of 1D objects. Upon order the dimensionality of system changes into 3. In the AF state, near T_N , the temperature dependence of the internal static fields follows the expectations of a 3D Ising model with an effective $S = 1/2$. The magnetic structure is characterized by a wave-vector $\vec{k}_{AF} = (0, 0, 1)$, independent of temperature and external magnetic field. The moments of 2.18 μ_B per Co ion are arranged AF within the screw chains, along the c axis, and in the basal planes they form ferromagnetic zig-zag paths along one of the axis and antiferromagnetic paths along the orthogonal (equivalent) direction.

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